## The Synthetic Longitudinal Business Database

Based on presentations by Kinney/Reiter/Jarmin/Miranda/Reznek²/Abowd on July 31, 2009 at the Census-NSF-IRS Synthetic Data Workshop
[link] [link]
Kinney/Reiter/Jarmin/Miranda/Reznek/Abowd (2011) "Towards Unrestricted Public Use Microdata: The Synthetic Longitudinal Business Database.", CES-WP-11-04

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## Overview

- LBD background
- Synthetic data generation
- Analytic validity
- Confidentiality protection
- Future plans


## Elements



## The ("Real") LBD

- Economic census covering nearly all private non-farm business establishments with paid employees
- Contains: Annual payroll and Mar 12 employment (1976-2005), SIC/NAICS, Geography (down to county), Entry year, Exit year, Firm structure
- Used for looking at business dynamics, job flows, market volatility, international comparisons...


## Longitudinal Business Database(LBD)

- Detailed description in Jarmin and Miranda
- Developed as a research dataset by the U.S. Census Bureau Center for Economic Studies
- Constructed by linking annual snapshot of the Census Bureau's Business Register (see Lecture 4)


## Longitudinal Business Database(LBD)

- CES constructed
- longitudinal linkages (using probabilistic matching, see Lecture 10),
- re-timed multi-unit births and
- dealt with missing data


## Access to LBD data

- Different levels of access
- Public use tabulations - Business

Dynamics Statistics http://www.ces.census.gov/index.php/bds

- "Gold Standard" confidential microdata available through the Census Research Data Center Network
- (LBD in RDC)
- Most used dataset in the RDCs


## Bridge between the two

- Synthetic data set
- Available outside the Census RDC
- Providing as much analytical validity as possible
- Reduce the number of requests for special tabulations
- Aid users requiring RDC access
- Experiment in public use business microdata


## Why synthetic data?

- Concerns about confidentiality protection for census of establishments
- LBD is a test case
- Criteria given for public release:
- No actual values of confidential values could be released
- Should provide valid inferences while protecting confidentiality


## Generic structure

- Gold standard: given by internal LBD (already completed)
- Partially synthetic:
- Unsynthesized:
- County (but not released!) [x1]
- SIC [x2]
- Synthesized
- Birth [y1] and death [y2] year:
- Multi-unit status [y3]
- Employment (March 12) [y4]
- Payroll [y5]


## Synthesis: General Approach

- $Y=[y 1|y 2| y 3|y 4| y 5]$
- $X=[x 1 \mid x 2]$
- Generate joint distribution of $\mathrm{Y} \mid \mathrm{X}$ by sampling from conditionals

$$
-f(y 1, y 2, y 3 \mid X)=f(y 1 \mid X) \cdot f(y 2 \mid y 1, X) \cdot f(y 3 \mid y 1, y 2, X)
$$

- Use SIC as "by" group


## General approach to synthesis

- Drawing from $f\left(y_{k} \mid X, y_{1}, \ldots, y_{k-1}\right)$
- Fit model using observed data
- Draw new values of parameters from posterior distributions
- Use new parameters to predict $y_{k}$ from $X$ and synthetic values of $\mathrm{y}_{1}, \ldots, \mathrm{y}_{\mathrm{k}-1}$


## SRMI approach

- Calendar:
- Step1: Impute y1 | X
- Step 2: Impute y2 | [y1|f(X)]
- Where $\mathrm{f}(\mathrm{X})$ uses state [ $\left.\mathrm{x} 1^{\prime}\right]$ instead of county $[\mathrm{x} 1$ ]
- Type of firm
- Step 3: Impute y3 | [y1|y2|X]
- Characteristics
- Step 4: Impute $\mathrm{y} 4(\mathrm{t}) \mid[\mathrm{y} 1|\mathrm{y} 2| \mathrm{y} 3|\mathrm{y} 4(\mathrm{t}-1)| \mathrm{x} 2]$
- Step 5: Impute $\mathrm{y} 5(\mathrm{t}) \mid[\mathrm{y} 1|\mathrm{y} 2| \mathrm{y} 3|\mathrm{y} 4(\mathrm{t})| \mathrm{y} 5(\mathrm{t}-1) \mid \mathrm{x} 2]$


## First Year

- Impute y1 (Firstyear) | SIC, County using variant of Dirichlet-Multinomial
- "Prior" information is obtained by collapsing categories
- Synthetic values obtained from sampling from multinomial distribution


## Last Year

- Impute y2 (Last Year)| First Year, State, SIC
- Simple multinomial approach
- Dirichlet-multinomial with flat prior
- Sample from multinomial probabilities obtained from matching categories in observed data


## Multi-unit Status

- Impute in two stages:
-Categorical response: Always MU, sometimes MU, never MU
- Imputed using simple multinomial approach
- Given change in status occurs, impute when change occurred (future)


## Employment and Payroll

- Highly skewed longitudinal continuous variables
- Imputed using a set of normal linear models with kde transformation of response (Abowd and Woodcock, 2004)
- Impute year by year, employment and then payroll, based on groups
- (3-digit SIC)
- by (multiunit status)
- by (continuer status)
- by (top $5 \%$ status)
- If model too sparse, use 2-digit SIC as prior


## Analytic Validity Tests

- Compare observed data and synthetic data for whole LBD
- Job creation and destruction
- Employment volatility
- Gross employment levels


## Job Creation Rates: LBD and Implicates by Year




## Job Creation from Births: LBD and Implicates by Year



Job Creation from Births and Expansions: LBD and Implicates by Year


Year
$\longrightarrow$ LBD $\quad$ Implicate 1 $\quad$ Implicate $2 \ldots$ Implicate (Mean)


## Employment Volatility: Establishment by Year, weighted





Figure 3: Share of Employment by Industry Sector and Year, 1976-2000


Figure 2: Share of Establishments by Industry Sector and Year, 1976-2000.


Figure 4: Share of Payroll by Industry Sector and Year, 1976-2000

$$
E M P_{i}=\alpha+\beta E M P_{i-1}+\delta P A Y_{i}+\theta I N D_{i}+\psi S T A T E_{i}+\vartheta A G E_{i}+\gamma M U_{i}+\epsilon
$$



Figure 11: Regression Coefficients, LBD vs Synthetic

## Confidentiality Protection

- Unavailable in SynLBD v2
- Firm structure
- firm linkages (across time, across implicates)
- Geography
- Basic protection
- replacing sensitive values of with draws from probability distributions


## Disclosure analysis

- High probability that an individual establishment's synthetic birth/death year is different from its actual birth/death year
- Synthetic maxima not necessarily near actual
- High between-imputation variability at establishment level


## Synthesizing Firstyear (Birth) and Lastyear (Death)

- Positive probability exists of producing any feasible birth year, and substantial probability exists that synthesized firstyear is not the actual firstyear
- Table on next slide shows this: prob(actual birth year=synthetic birth year I synthetic birth year) is low
- Similar results hold for deaths
- Conclusions: establishment lifetimes are random, so users can't accurately attach establishment identifications to them


## Summary Data:

| Observed Establishment Births Occuring in Same Yearas Synthetic Births |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| First (Birth) Year |  | Percent of Biths Over Industries |  |  |
| Synthetic | Actual | Minimum\| | Mean\| | Maximum |
| 1975 | 1975 | 1.52 | 25.41 | 88.89 |
| 1976 | 1976 | 0.12 | 5.12 | 75.00 |
| 1977 | 1977 | 0.43 | 5.09 | 71.43 |
| 1978 | 1978 | 0.46 | 3.65 | 16.22 |
| 1979 | 1979 | 0.27 | 3.89 | 50.00 |
| 1980 | 1980 | 0.36 | 3.46 | 25.00 |
| 1981 | 1981 | 0.26 | 3.91 | 50.0 |
| 1982 | 1982 | 0.36 | 3.69 | 50.00 |
| 1983 | 1983 | 0.39 | 4.10 | 50.00 |
| 1984 | 1984 | 0.69 | 3.79 | 19.30 |
| 1985 | 1985 | 0.15 | 3.75 | 23.73 |
| 1986 | 1986 | 0.41 | 3.92 | 33.33 |
| 1987 | 1987 | 0.35 | 4.19 | 25.00 |
| 1988 | 1988 | 0.48 | 4.25 | 52.4 |
| 1989 | 1989 | 0.63 | 4.28 | 25.15 |
| 1990 | 1990 | 0.47 | 3.91 | 25.00 |
| 1991 | 1991 | 0.56 | 4.18 | 50.00 |
| 1992 | 1992 | 0.45 | 3.94 | 17.39 |
| 1993 | 1993 | 0.67 | 3.86 | 25.00 |
| 1994 | 1994 | 0.53 | 4.33 | 50.00 |
| 1995 | 1995 | 0.35 | 4.16 | 16.67 |
| 1996 | 1996 | 0.20 | 4.11 | 16.67 |
| 1997 | 1997 | 0.10 | 4.04 | 18.60 |
| 1998 | 1998 | 0.46 | 3.85 | 20.00 |
| 1999 | 1999 | 0.28 | 4.64 | 43.02 |
| 2000 | 2000 | 0.31 | 4.46 | 33.33 |
| 2001 | 2001 | 0.35 | 4.22 | 25.27 |

## Example: Year of birth



## Confidentiality Protection: Breaking Firm Links

- Firm characteristics not synthesized
- Firm characteristics more skewed than establishment characteristics
- Cannot link multi-unit establishments to their firms


## Confidentiality Protection: Breaking Links Across Implicates

- Synthetic observations with the same LBDnum across implicates are not generated from the same LBD establishment
- Can't group (across implicates within year) observations generated from same establishment


## Confidentiality Protection: Synthesizing Employment and Payroll

- Synthesis models are essentially regressions with transformed variables
- Synthesis captures low-dimensional relationships and sacrifices higher-dimensional ones
- Synthesized employment and payroll vary substantially around regression lines
- Synthesized employment and payroll vary significantly from observed values


## Example: Correlations Among Actual and Synthetic Data

- SIC 573 - year 2000

| Pearson Correlation Coefficients <br> SIC 573 <br> Year: 2000 |  |  |  |  |
| :--- | ---: | :--- | :--- | :--- |
|  | Employment | Synthetic <br> Employment | Payroll | Synthetic <br> Payroll |
| Employment | 1 |  |  |  |
| Synthetic | 41000 |  |  |  |
| Employment | 0.003 | 1 |  |  |
| Payroll | 21100 | 41000 |  |  |
| Synthetic | 0.712 | -0.012 | 1 |  |
| Payroll | 41000 | 21100 | 41000 |  |

## Correlations of observed vs synthetic Employment

Type $=$ Pearson


## Correlations of observed vs synthetic Payroll

## Type $=$ Pearson



## Conclusions

- Analytical validity supported for broad analyses
- Issues with some details
- Obtain user feedback to inform future refinements
- Sufficient confidentiality protection
- Basic metrics show strong protection
- Differential privacy protection not yet verified


## Ongoing work at Census

- Include NAICS, geography, changes in multiunit status, firm age \& size
- Multiple Imputations for release
-Address bias in job creation/destruction
- Extend time series

